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Aparna Venkatesan University of San Francisco, avenkatesan@usfca.edu

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THE OPTICAL DEPTH TO REIONIZATION AS A PROBE OF COSMOLOGICAL AND ASTROPHYSICAL PARAMETERS

Aparna Venkatesan

Department of Astronomy and Astrophysics, 5640 South Ellis Avenue, University of Chicago, Chicago, IL 60637; aparna@oddjob.uchicago.edu Received 1999 December 17; accepted 2000 February 8

ABSTRACT

Current data of high-redshift absorption-line systems imply that hydrogen reionization occurred before redshifts of about 5. Previous works on reionization by the first stars or quasars have shown that such scenarios are described by a large number of cosmological and astrophysical parameters. Here we adopt a semianalytic model of stellar reionization in order to quantify how the optical depth to reionization depends on such parameters, and combine this with constraints from the cosmic microwave background (CMB). We find this approach to be particularly useful in alleviating the well-known degeneracy in CMB parameter extraction between the optical depth to reionization and the amplitude of the primordial power spectrum, due to the complementary information from the reionization model. We also examine translating independent limits on astrophysical parameters into those on cosmological parameters, or, conversely, how improved determinations of cosmological parameters can constrain astrophysical unknowns.

Subject headings: cosmic microwave background — early universe — intergalactic medium — stars: formation

1. INTRODUCTION

Observations of the spectra of distant quasars and galaxies have revealed the absence of a Gunn-Peterson trough, implying that the intergalactic medium (IGM) was highly ionized by redshifts of about 5. Since the universe recombined at redshifts $z \sim 1100$, the IGM is expected to remain neutral until it is reionized through the activity of the first luminous sources. At present, it appears that the reionization of hydrogen occurred before $z \sim 5$ (Schneider, Schmidt, & Gunn 1991; Hu, McMahon, & Cowie 1999; Spinrad et al. 1998), while that of doubly ionized helium is thought to have occurred before $z \sim 3$ (Hogan, Anderson, & Rugers 1997; Reimers et al. 1997).

The ionizing sources responsible for reionization can be a variety of astrophysical objects, and much work has been done on reionization by the first stars (Haiman & Loeb 1997; Fukugita & Kawasaki 1994), the first quasars (Haiman & Loeb 1998a; Valageas & Silk 1999), protogalaxies (Cen & Ostriker 1993; Gnedin 2000; Giroux & Shapiro 1996; Ciardi et al. 2000; Miralda-Escude, Haehnelt, & Rees 2000; Madau, Haardt, & Rees 1999), and related phenomena such as supernova-driven winds (Tegmark, Silk, & Evrard 1993) and cosmic rays (Nath & Biermann 1993). Quasars are natural candidates for both H I and He II reionization, since they are more luminous and provide harder ionizing radiation than stars, and they are seen up to the highest redshifts of current observations. However, there are indications of a turnover in the space density of the QSO population, which apparently decreases beyond $z \sim 3$. Since this is based on optical surveys, this observed decline is subject to the effects of any dust obscuration along the line of sight; however, recent radio observations also appear to indicate a declining QSO population beyond $z \sim 3$, so that the comoving emission rate of Lyman-continuum photons from QSOs is deficient by a factor of ~ 4 relative to that required for reionization (see, e.g., Madau 1998 and references therein). If this is real, then QSOs may be less plausible as sources for H I reionization (see also Rauch et al. 1997). The alternative is to allow QSO

formation in collapsing halos from the outset, and to postulate a large population of faint QSOs at $z \gtrsim 5$, with the observed turnover being true for bright QSOs only.

Stellar reionization is attractive for several reasons. The first stars are expected to form at $z \gtrsim 10$, and are capable of ionizing hydrogen. Furthermore, they create heavy elements, and may account for the low $(0.01 Z_{\odot})$ but persistent metallicity seen in the Ly α forest clouds out to $z \sim 4$. Finally, the detections of a He II absorption trough in high-z quasar spectra appear to indicate a soft component to the UV background (Haardt & Madau 1996), consistent with the ionizing spectrum of stars.

Early work on hydrogen reionization (Arons & Wingert 1972) described the appearance of the first luminous sources, about which ionized bubbles gradually expand into a neutral IGM; eventually, such H II regions overlap and the universe becomes transparent to Lyman-continuum photons. In principle, only one ionizing photon per neutral atom in the IGM is required, but the effects of recombinations ensure that for an atom to stay ionized, the rate of ionizing photons generated by sources must be greater than the rate of recombination at that epoch. This is of particular importance at high z, when the IGM had greater density. Just how much more than 1 photon per baryon is needed is a function of the cosmology and the assumptions of the reionization treatment; some evolution with redshift is also expected. A qualitative assessment can be made, however; for example, from arguments of producing the average IGM metallicity in C IV of about $10^{-2} Z_{\odot}$ at $z \leq 5$, Miralda-Escude & Rees (1997) arrived at a requirement of 20 ionizing photons per baryon. For the stellar reionization model that will be considered in this work, we will see below that about 5 ionizing photons per baryon are available for H I reionization and prove sufficient. Not more than a few percent of all baryons need to participate in early star formation for reionization to occur by $z \sim 5$, although this number may reach values of up to about 15% (§ 2).

Although reionization by early stars would occur at redshifts well beyond current observations, it has many distinct

consequences that can be feasibly constrained by current and future experiments. Some of these include, as mentioned above, the evolving IGM metallicity and the cosmic ionizing background as derived from spectral features in high-z absorption-line systems. High-z reionization will also leave a signature in the CMB through the Thomson scattering of CMB photons from free electrons (Sugiyama, Silk, & Vittorio 1993; Dodelson & Jubas 1995; Tegmark, Silk, & Blanchard 1994; Tegmark & Silk 1995; Hu 2000; Zaldarriaga 1997). Depending on the epoch and degree of reionization, we expect an overall (somewhat scaledependent) damping of primary temperature anisotropies in the CMB, the generation of new temperature anisotropies on the appropriate scales through the effects of secondorder processes and the degree of inhomogeneity in the reionization process (Gruzinov & Hu 1998; Knox, Scoccimarro, & Dodelson 1998), and finally, the creation of a new polarization signal, as the process of Thomson scattering introduces some degree of polarization even for incident radiation that is unpolarized. Scattering from the ionized IGM, or the reprocessing of starlight into far-infrared wavelengths by dust formed from early supernovae (SNe), will also cause the CMB to undergo some spectral distortion (Loeb & Haiman 1997); this can be measured experimentally through the Compton y-parameter. These and other observational signatures that have the potential to constrain the epoch, and hence possibly the source, of reionization have been examined in the literature (see Haiman & Knox 1999 for a summary).

A model of reionization is therefore, in principle, eminently testable. Current detections of the first Doppler peak in the CMB's temperature anisotropies limit the total optical depth to electron scattering, τ_e , such as may arise from reionization, to be $\tau_e \leq 1$ (Scott, Silk, & White 1995). Future experiments such as the Next Generation Space Telescope (NGST) or the Space Infrared Telescope Facility (SIRTF) may detect the high-z sites of reionizing sources (see, e.g., Haiman & Loeb 1998b), or at least exclude currently viable candidates, while upcoming CMB experiments such as MAP or the Planck surveyor can measure τ_e to very high accuracies by combining information from temperature anisotropies and polarization in the CMB.

The optimistic prospects for testing reionization and the increasing multiwavelength view of the high-z universe have generated a large body of work on reionization models in the last few years, whose techniques fall broadly into numerical (Gnedin 2000; Chiu & Ostriker 2000; Gnedin & Ostriker 1997; Cen & Ostriker 1993) or semianalytic methods (Haiman & Loeb 1997, 1998a; Tegmark et al. 1994; Valageas & Silk 1999). The former have the advantage of being able to track the details of radiative transfer, incorporating the clumpiness of the IGM and the essentially nonuniform development of ionizing sources, and, perhaps most importantly, describing the process of reionization in a quantitative fashion. The advantage of semianalytic approaches is their inherent flexibility and ability to probe the parameter space of a reionization model at will, which is of value given the many input cosmological and astrophysical parameters involved.

For astrophysical sources, the process of reionization is strongly related to the evolution of structure in the universe, and could result in feedback effects for subsequent object formation (see, e.g., Ciardi et al. 2000). Of the current theories of structure formation, variants of the standard cold dark matter (SCDM) model are considered to be relatively successful at describing the observed universe. This picture postulates a critical-density universe, with cold dark matter dominating the matter content; structures, made up of baryons and CDM, originated in primordial adiabatic fluctuations and evolved subsequently through gravitational instability. Current modifications to this paradigm include, e.g., the addition of a cosmological constant.

The SCDM model, and its variants, are described by a set of parameters that characterize the primordial power spectrum of fluctuations, the cosmology of the universe, and quantities related to primordial nucleosynthesis. At present, the extraction of such parameters from observations has been made feasible by the quality of data from large-scale structure surveys, from cosmic velocity flows (Zehavi & Dekel 1999), from Type Ia SNe (Tegmark 1999), and from current and projected future data from the CMB (Zaldarriaga, Spergel, & Seljak 1997; Eisenstein, Hu, & Tegmark 1999). Typically, a 9-13 parameter set describes the adiabatic CDM model, and can be solved for given the data. One of these parameters is τ_e , which is by nature somewhat unique, in that it is the only quantity that is not set purely by the physics prior to the first few minutes after the Big Bang. Thus, it can potentially provide clues as to postrecombination astrophysics, assuming that the other (cosmological) parameters that also affect τ_e are comparatively well constrained.

Several of the semianalytic works on reionization mentioned above have explored the effects on τ_e of varying model parameters. Other authors have performed CMB analyses that have revealed inherent degeneracies in constraining specific combinations of parameters, e.g., τ_e and the amplitude of the primordial power spectrum, A (see, e.g., Zaldarriaga et al. 1997; Eisenstein et al. 1999). In this paper, we examine the results of cross-constraining the range in a cosmological parameter, given the allowed band in τ_e from a reionization model due to astrophysical parameter uncertainty, with the permitted range from CMB observations. Specifically, we find that for the combination τ_e -A, the wellknown degeneracy in their effects on the CMB can be broken when used in combination with the constraints from a reionization model. Since τ_e depends on both cosmological and astrophysical parameters, however, such an analysis can be extended to mutual constraints involving these two independent classes of parameters, by eliminating τ_e . The advantage of this is that, given a model of structure formation and a reasonable framework describing reionization, as well as the data from the CMB, we can use known astrophysics to further constrain cosmology and place tighter limits on cosmological parameters, even those that will be determined to high accuracies by future experiments. Conversely, a well-determined cosmological parameter can be used to constrain the astrophysics of ill-known details of early star formation. This will, at the least, be a powerful test of the cosmology, if our understanding of reionization is reasonably correct; the additional hope is that this will prove to be an alternative way of constraining the activity of the first stars.

The plan of the paper is as follows. In § 2, we outline the stellar reionization scenario that we consider, and set up a parameter set that describes reionization. In § 3, we review the standard methodology related to parameter extraction from the CMB, and incorporate the parameter set from § 2 into this formalism. In § 4, we present our results, and show

the combined constraints from a reionization model and the CMB. We present our conclusions in \S 5.

2. THE STELLAR REIONIZATION MODEL

We assume a SCDM primordial power spectrum of density fluctuations, given by $P(k) = Ak^n T^2(k)$, where A and *n* are, respectively, the amplitude and index of the power spectrum, and where the matter transfer function, T(k), is taken to be of the form given in Bardeen et al. (1986), with the baryon correction as given by Peacock & Dodds (1994). Here we evaluate the power-spectrum normalization Athrough the value of the rms density contrast over spheres of radius 8 h^{-1} Mpc today, σ_8 . The cosmology of our model is also described by Ω_0 , the cosmological density parameter; Ω_b , the density parameter of baryons; and *h*, the Hubble constant in units of 100 km s⁻¹ Mpc⁻¹. We assume that $\Omega_0 = 1$ throughout this work, and thus do not include it in the parameter set to be varied in what follows. We assume that there are no tensor contributions to P(k), and set the cosmological constant to be zero. Thus, our cosmological parameter set is (A, n, Ω_b, h) .

The reionization of the universe by the first generations of stars is described by the model developed in Haiman & Loeb (1997, hereafter HL97), with the minor modifications described below. Briefly, the fraction of baryons in collapsed dark matter halos, F_B , is followed using the Press-Schechter formulation; of these baryons, a fraction f_* cool and form stars in a Scalo initial mass function (IMF). A fraction f_{esc} of the generated ionizing photons is assumed to escape from the host object and propagate isotropically into the IGM. One can then solve for the size of the ionized regions associated with each such star-forming cloud, which, when integrated over all haloes, yields at each z the average ionization fraction of the universe, given by the filling factor of ionized hydrogen by volume $(F_{H II})$. We assume that the IGM is homogeneous, in which case the ionized region created by each source can be taken to be spheres of radius r_i . Reionization is defined to occur when $F_{\rm H\,II} = 1$. The total optical depth for electron scattering, $\tau_{\rm reion}$, to the reionization redshift, $z_{\rm reion}$, is given by integrating the product of the electron density, the ionization fraction, and the Thomson cross section along the line of sight from the present to z_{reion} . The cosmology of the universe enters τ_{reion} through the first two terms of the integrand, and also through the path length of the photons last scattered at z_{reion} .

Our adopted model is summarized by the following equations for an $\Omega_0 = 1$ universe:

$$F_B(z) = \operatorname{erfc}\left[\frac{\delta_c}{\sqrt{2}\sigma(R, z)}\right],\tag{1}$$

$$F_{\rm H\,II}(z) = \rho_B(z) \int_{z_*}^z dz_{\rm on} \frac{dF_B}{dz} (z_{\rm on}) \left[\frac{4\pi}{3M} r_i^3(z_{\rm on}, z) \right], \quad (2)$$

$$\tau_{\rm reion} = 0.053\Omega_b h \int_0^{z_{\rm reion}} dz \sqrt{1+z} [1-f_*F_B(z)] F_{\rm H\,II}(z) \,. \quad (3)$$

The critical overdensity, $\delta_c \equiv 1.686$, $\sigma(R, z)$ is evaluated with a spherical top-hat window function over a scale $R \propto M_C$, where M_C is the minimum halo mass that collapses at a given redshift. While a natural choice for M_C is the baryonic Jeans mass, given by $\sim 10^6 M_{\odot} [(1 + z)/100]^{1.5}$, this assumes that collapsing halos at a given mass scale are equivalent to star-forming halos. However, several authors (Tegmark et al. 1997; Haiman, Rees, & Loeb 1996) have argued for a higher value of M_c , based on the requirement of an effective coolant for baryons in a halo to fragment into stars. The picture is as follows: the very first stars form from metal-free gas and cool through primordial molecular hydrogen. The universe at that epoch is transparent to photons in the energy range 11.2–13.6 eV, but is opaque to more energetic photons. This initial trace level of stellar activity easily photodissociates the remaining H₂ in the universe (whose abundance relative to H I is very low), well before the H I ionizing flux has built to values sufficient for reionization (see HL97 and references therein). Subsequent halo formation continues, but star formation halts since there is no coolant available, and can only resume when halos more massive than $10^8 M_{\odot}[(1 + z)/10]^{-1.5}$ collapse, which can utilize line cooling by atomic H. We set M_c to be this higher value, with the understanding that F_B now represents the fraction of all baryons that are in star-forming halos. Finally, z_* is the earliest redshift at which the first stars can form, and here we set it to be 100. Prior to this, the temperature of the IGM is coupled to that of the CMB, and the CMB photons are still energetic enough to photodestroy H^- , thus preventing the formation of H_2 through the H⁻ channel, an important cooling mechanism for structures at these high redshifts to fragment into stars.

The evolution of an individual ionization front is characterized by the ionization radius r_i , and, for a time-dependent source luminosity, can be solved for through a differential equation as in HL97, where the rate of emission of ionizing photons from a stellar population of metallicity $Z = 10^{-1}$ Z_{\odot} was constant for about 2 Myr before declining with the death of the massive stars in the IMF. In this work, we use the analytic solution from Shapiro & Giroux (1987; hereafter SG87) for the evolution of r_i in an expanding universe in units of the Strömgren radius, rs. The Strömgren radius represents the equilibrium reached in the IGM between a source's ionizing photon rate and the IGM's recombination rate; r_s increases with decreasing z, or equivalently, with decreasing average IGM density. The maximum value that r_i can have is r_s ; only sources at very high redshifts (~100) have ionized regions that fill their Strömgren spheres (SG87). Note that since the SG87 solution does not account for time-varying sources, we expect τ_{reion} to be overestimated (reionization occurs earlier) compared to HL97, but as we show in the next section, this is a very slight effect. Thus, in this work, $r_i = (r_i/r_s)_{SG87} r_s$, where $r_s^3 = 3S(0)/[4\pi\alpha_B n_H^2(z)]$, $\alpha_B = 2.6 \times 10^{-13} \text{ cm}^3 \text{ s}^{-1}$, and the initial emission rate of ionizing photons leaving the host object is S(0). Here $F_{\rm H\,I}(z)$ (see eq. [2]) is determined at each redshift z by integrating over the product of the rate of new halos that formed stars at a turn-on redshift z_{on} (where $z < z_{on} <$ z_*) and the ionized volume per unit mass associated with such objects, for a source mass M. A detailed treatment of the evolution of F_B and $F_{H \pi}$ with z, given various choices of input parameters, can be found in HL97. For their standard model, F_B rises rapidly, from values of $\sim 10^{-3}$ at $z \sim 20$ to about 0.1 at $z \sim 10$; during this period, $F_{\rm H\,\pi}$ rises steeply from about 10^{-4} ($z \sim 32$) to unity at $z \sim 18$, so that reionization occurs relatively quickly with the growth of F_B .

We now see that τ_{reion} is a function of several cosmological and astrophysical parameters. The astrophysical parameter set is $(f_*, M_C, S(0))$. The parameter S(0) is itself a function of several variables: the choice of the IMF, the metallicity Z of the progenitor stars, f_{esc} , f_* , and the halo's

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mass. The last two factors account for the fraction of starforming baryons in each halo, while f_{esc} represents the loss of ionizing photons to the host cloud before reaching the IGM. Let us now consider the first two variables. Although there have been some arguments for the IMF to be biased toward high-mass stars in the early universe (Larson 1998), the details of the nature of star formation under those conditions are still not well understood. In the absence of a convincing theory of primordial star formation, the most reasonable assumption is to take a present-day IMF and calculate the luminosity expected from metal-poor stars. Since reionization is affected primarily by the massive stars in any IMF, an IMF in the past biased toward high-mass stars would still have the same emission spectrum of ionizing photons, while one dominated by low-mass stars is unlikely to reionize the universe by $z \sim 5$. We therefore take S(0) to be as given in HL97 for $Z = 10^{-4} Z_{\odot}$ stars from standard stellar evolutionary models; it includes the ionizing radiation from stars only, and is steady at $f_* f_{\rm esc} \times 10^{46}$ photons s⁻¹ M_{\odot}^{-1} for about 2 Myr before declining rapidly, which is consistent with the value in, e.g., Ciardi et al. (2000). As a rough estimate, this translates to ~ 5 ionizing photons per baryon in the universe, for $f_* = 0.05$, $f_{\rm esc} = 0.2.$

The ionizing photon contribution from SNe is relatively small (HL97), but most of the mass assigned to forming stars is eventually returned to the IGM. Therefore, the second factor on the right-hand side of equation (3) for τ_{reion} should have an extra contribution, $f_{SN} f_* F_B$, to account for the extra baryons that are available for new star formation, where f_{SN} is an IMF-averaged fraction of the progenitor mass that is expelled into the IGM at the end of the star's life. We expect between $\sim 50\%$ and 95% of the parent star's mass as ejecta, until a point is reached (for stellar masses ranging from 50 to 100 M_{\odot}) where the entire star collapses into a black hole. For the low values of f_* that will be considered here, the product $f_* f_{sN}$ will be a small correction and can be ignored. Moreover, the mass of the ejecta from a dying star depends sensitively on the stellar metallicity, with low-Z stars having higher remnant masses and less ejected material relative to solar-Z stars (Woosley & Weaver 1995). Thus, f_{SN} is likely to be highly variable, both spatially and with z, due to the evolving metallicity of subsequent generations of stars, and is more appropriately modeled in a simulation rather than in a semianalytic model. The calculated values of τ_{reion} here can be taken as a lower limit.

This leaves the astrophysical parameters, f_* , $f_{\rm esc}$, and M_C . We note that in most semianalytic models, f_* is set by the choice of M_C , since the stellar Z output, particularly in ¹²C, is combined with the evolution of F_B to produce the observationally detected average carbon abundance of 0.01 Z_{\odot} in the Ly α forest clouds at $z \sim 3$ (Songaila & Cowie 1996). Thus, f_* and M_C are not independent of each other if we choose the above normalization; for the HL97 choice of M_C , $f_* = 0.13$. This is the maximum value that f_* can have from arguments of avoiding IGM overenrichment; given the approximately order-of-magnitude scatter in the average metal abundance of the Ly α clouds, and that one need not require the reionizing stars to solely account for $Z_{\rm IGM}$, f_* may be smaller than ~ 0.15 .

As an aside for the interested reader, we note here two drawbacks of normalizing f_* via ¹²C. One is that the massive stars in the IMF ($\gtrsim 10 M_{\odot}$) are the ones relevant for reionization, while ¹²C is produced dominantly by the

intermediate-mass stars (2–8 M_{\odot}). Thus, if the IMF was different in the past, the carbon abundance in the $Ly\alpha$ forest does not constrain the massive or reionizing stellar activity in early halos. The second point to note is that the pause in star formation caused by the initial dissociation of H_2 led to the choice of M_c , as in HL97. This minimum halo mass corresponds to objects with virial temperatures of $\sim 10^4$ K. At this temperature, the host object is immune to photoionization heating (as pointed out in HL97), and so if outflows are desired to expel the generated metals into the IGM (i.e., the Ly α forest), the mechanical energy of SNe must be invoked. Again, the massive reionizing stars end their lives as Type II SNe an order of magnitude in time before their intermediate-mass carbon-producing compatriots. Since all the mechanical input lies with Type II SNe, the question arises of how the carbon, produced significantly later, leaves the host halo to mix with the IGM. Furthermore, Type II SNe occur on much more predictable timescales, i.e., immediately following the progenitor's death, than do Type Ia SNe (3–10 Gyr), and there is not much more than a wheeze to be had from the deaths of intermediate-mass stars as planetary nebulae.

Having voiced these objections, we point out that while the ¹²C connection as made above between M_C and f_* is not ideal, postulating a general relation between these two variables is not ad hoc. The value of M_C does intrinsically determine the stellar history, metallicity, and luminosity evolution of the universe; the high value of M_C in HL97 and other works is physically well-motivated by the necessary step of having an available coolant to aid star formation. We proceed to set $M_C = 10^8 M_{\odot}[(1 + z)/10]^{-1.5}$ for the semianalytic treatment here, and now narrow our astrophysical parameter set to (f_{esc}, f_*) .

We end here by addressing some of the issues that are not accounted for in this work. The IGM is assumed to be homogeneous, but clearly some clumpiness will develop in the IGM from the growth of initial density inhomogeneities, and the assumption of the average ionized fraction at a given redshift being equal to the H II filling factor will eventually break down. However, this appears to be a relevant effect only at "late" times ($z \leq 10$), when the fraction of baryons in collapsed structures becomes significant (Gnedin & Ostriker 1997), or for baryon-dominated universes (SG87). Therefore, we assume that the clumping factor is unity (homogeneous IGM) for the rest of this work. We have also neglected corrections from doubly ionized helium, which is not problematic, since the spectrum of photons produced by stars is softer than that from quasars, and is more relevant for H I than for He II reionization (see, however, Tumlinson & Shull 2000 on the helium-ionizing spectrum from zero-metallicity stars). We have set $F_{\text{He II}} =$ $F_{\rm H\, II}$, but this introduces an error of not more than a few percent (Tegmark & Silk 1995). Finally, we have not included the effects of bias in the normalization of the matter power spectrum, i.e., we assume that light traces the underlying mass distribution.

3. CONSTRAINTS FROM THE MICROWAVE BACKGROUND

As discussed in the introduction, signatures from reionization are expected in the CMB; an accurate measurement of τ_{reion} or the detection of postrecombination features in the CMB anisotropies have the power to constrain the reionization epoch and the nature of the sources through the angular scale $\theta(\propto l^{-1})$ on which they affected the CMB. Here l is defined from expanding the angular power spectrum of the CMB in terms of its multipole moments C_l and Legendre polynomials:

$$C(\theta) \equiv \sum_{l=2}^{\infty} \frac{(2l+1)}{4\pi} C_l P_l(\cos \theta) .$$
(4)

The effect of τ_{reion} is to introduce an overall damping of the temperature C_l 's (HL97, and references therein), except at the largest scales. As discussed by, e.g., Zaldarriaga et al. (1997), this is practically indistinguishable from the generally reduced values of C_l expected from simply having a lower amplitude, A, of the primordial power spectrum; the difference between these two effects at the smallest *l*'s is obscured by cosmic variance. While the amount of the damping due to τ_{reion} is *l*-dependent and can potentially break this degeneracy, the accuracy to which τ_{reion} can be estimated from temperature anisotropy maps alone is not sufficient to distinguish between these two different effects (Zaldarriaga 1997).

When combined with the polarization data from the CMB however, τ_{reion} can be constrained with far greater precision. Linear polarization is generated by the primary temperature quadrupole anisotropy photons scattering off the free electrons in the reionized IGM, and is a relatively clean probe of the epoch of reionization (Zaldarriaga 1997). The polarization signal is expected at low levels compared to that from temperature anisotropies, and may prove difficult to measure, especially for low optical depths. Nevertheless, τ_{reion} should be able to be detected, in principle, by future experiments to within 1 σ errors of, e.g., 0.69 without polarization (0.022 with polarization) information for *MAP*, and 0.59 (0.004) correspondingly for *Planck* (Eisenstein et al. 1999).

We wish to combine the constraints on cosmological or astrophysical parameters from a reionization scenario with those from the CMB; in order to do this for the latter, we follow the standard prescription as outlined in, e.g., Jungman et al. (1996) and Knox (1995). We assume Gaussian initial perturbations, and that the multipole moments C_1 are determined by a "true" set of N theoretical parameters, (P_N) . If we define the likelihood function \mathscr{L} of observing a set of C_l 's, given P_N , then the behavior of \mathscr{L} near its maximum can be quantified in terms of the Fisher information matrix, whose elements are given by the second derivative of the logarithm of \mathscr{L} with respect to pairs of parameters in P_N . The Fisher matrix then represents the accuracy with which P_N can be estimated from a given data set; here, the CMB's experimentally measured C_1 's. Further assuming that \mathscr{L} has a Gaussian form near its maximum, the Fisher matrix is given by

$$F_{ij} = \sum_{l=2}^{\infty} \frac{1}{\sigma_l^2} \left[\frac{\partial C_l(P_N)}{\partial P_i} \frac{\partial C_l(P_N)}{\partial P_j} \right], \quad 1 \le i, j \le N , \quad (5)$$

where σ_l is a measure of how the observed C_l 's are distributed about the mean value of the true $C_l(P_N)$'s. We assume that σ_l is cosmic variance limited, and we ignore terms arising from the instrumental noise associated with an experiment and from any foregrounds. For a sky fraction $f_{\rm sky}$ that has been mapped, σ_l can be approximated by

$$\sigma_l = \begin{cases} \sqrt{\frac{2}{(2l+1)f_{sky}}} C_l(P_N) & l \le l_{max} \\ \infty & l > l_{max}. \end{cases}$$
(6)

systematic effects, the power of the C_l 's to constrain P_N , as presented here, is the "best possible" case. Note also that the above formulae are valid when only the temperature information from the CMB is used. More general expressions for the case of including polarization data can be found in, e.g., Zaldarriaga et al. (1997). The derivatives of the C_l 's with respect to P_N were com-

The derivatives of the C_l 's with respect to P_N were computed for each parameter using two-sided derivatives with step sizes chosen so that the value of this derivative remained stable (see, e.g., Eisenstein et al. 1999, Appendix B.1). The values of the C_l 's themselves for a given parameter set were found using the publicly available CMBFAST code (version 2.4.1).¹ Note that the parameter set describing the reionization model is $(A, \Omega_b, h, n, f_{esc}, f_*)$, which yields τ_{reion} , whereas the CMB data can determine the cosmological parameters and τ_{reion} , or equivalently, $[P_{cosmo}, \tau_{reion}(P_{cosmo}, P_{astro})]$. Therefore, when we specify τ (e.g., to CMBFAST), the cosmological and the astrophysical parameter sets (P_{cosmo}, P_{astro}) are no longer independent, but are related through the reionization model, and the C_l derivatives become

$$\frac{\partial C_l}{\partial P_{\text{cosmo}}} = \frac{\partial C_l}{\partial P_{\text{cosmo}}} \bigg|_{\tau} + \frac{\partial C_l}{\partial \tau} \bigg|_{P_{\text{cosmo}}} \frac{\partial \tau}{\partial P_{\text{cosmo}}}, \quad (7)$$

$$\frac{\partial C_l}{\partial P_{\text{astro}}} = \frac{\partial C_l}{\partial \tau} \frac{\partial \tau}{\partial P_{\text{astro}}} \,. \tag{8}$$

Once the Fisher matrix, F_{ij} , has been constructed, it can be inverted to give the covariance matrix \mathscr{C} between the parameters P_N ; \mathscr{C}_{ii} represents the minimum variance in the estimate of P_i . Any 2 × 2 submatrix of \mathscr{C} can then be extracted, giving the ellipse equation for the joint confidence region in the two-parameter subspace of interest,

$$[\boldsymbol{P} - \boldsymbol{P}_N] \cdot (\mathscr{C}_{2 \times 2})^{-1} \cdot [\boldsymbol{P} - \boldsymbol{P}_N] = \Delta , \qquad (9)$$

where Δ is set throughout this work to be at the 68% confidence level. 4. RESULTS

We present our results here from combining the reionization model (§ 2) and the constraints from the CMB (§ 3). This analysis assumes that the density perturbation spectrum at the CMB and structure formation scales is described by the same power law. For the choice of parameters in HL97, where $f_* = 0.13$ and $f_{\rm esc} = f_{\rm esc}(z)$, we obtain $\tau_{\rm reion} = 0.0734$, or $z_{\rm reion} \sim 18.4$, which only slightly exceeds the HL97 value of $\tau_{\rm reion} = 0.07$. Henceforth, we will refer to $\tau_{\rm reion}$ as τ for convenience, noting that τ is always evaluated to the reionization epoch in this work. We define our standard model (SM), fixing $\Omega_0 = 1$, as given by $A(\sigma_8 = 0.7) =$ 1.55×10^6 , $\Omega_b = 0.05$, h = 0.5, n = 1.0, $f_{\rm esc} = 0.2$, $f_* = 0.05$, and $\tau = 0.0573$, with reionization occurring at $z \sim 15.5$.

As a simple example, we begin with the τ -A plane, shown in Figure 1, where we isolate the dependence of τ on A, keeping all the other parameters in the SM fixed. The range of σ_8 is ~0.5–0.8, from the large-scale distribution of clusters of galaxies (see, e.g., Bunn & White 1997, and references therein), but is 1.2 when normalized to *COBE* for the SM choice of cosmological parameters. As an illustrative range

¹ CMBFAST is available at: http://www.sns.ias.edu/~matiasz/CMBFAST/cmbfast.html.

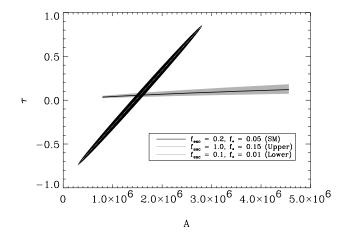


FIG. 1.—Combined constraints in the τ -A plane from the reionization model and current CMB data. The standard model (SM) is shown by the solid line; the shaded band represents the astrophysical uncertainty in the reionization model, given the allowed ranges for (f_{esc}, f_*) ; and the ellipse shows the 1 σ joint confidence region from current CMB data.

for the plots, we normalize A for $\sigma_8 = 0.5$ –1.2. The solid line in Figure 1 represents the SM, while the light-shaded region represents the uncertainty due to the astrophysics of the reionization model (or AS, for astrophysical slop), with $(f_{esc},$ f_*) = (1.0, 0.15) for the upper and (0.1, 0.01) for the lower envelope. The range for f_* (0.01–0.15) is set as follows: the lower limit comes from numerical simulations of star formation (see, e.g., Ciardi et al. 2000, and references therein), while the upper limit corresponds approximately to that in HL97 and Haiman & Loeb (1998a). The value of f_{esc} has been estimated through a number of theoretical and observational methods (see Wood & Loeb 2000, and references therein). Here, we take the range for $f_{\rm esc}$ to be 0.1–1.0, the lower limit coming from Dove, Shull, & Ferrara (2000, hereafter DSF), who modeled the escape fraction of ionizing photons from OB stellar associations in the H I disk of the Milky Way, and found that for a coeval star formation history, $f_{\rm esc} = 0.15 \pm 0.05$. Our choice of this limit from DSF is motivated by the similarity of their model's luminosity history to that in HL97; as noted above, there are alternate values for f_{esc} in the literature for a variety of astrophysical environments. We will use both the full range for f_{esc} and the more narrow DSF band in later plots.

To combine this with the CMB constraint, a shaded ellipse representing the two-parameter 68% joint confidence region is overplotted, assuming that the true model describing the universe is given by the SM and $[\tau, A] =$ $[0.057, A(\sigma_8 = 0.7)]$. This ellipse is narrow enough that we show a magnified version of Figure 1 in Figure 2, with an additional lighter band, nested within the AS band, showing the effect of varying only f_{esc} while fixing f_* to its SM value. We see that the CMB does not really constrain τ or A separately at all, a near degeneracy that was expected from the discussion in the previous section. However, the combination of the CMB confidence region and the AS band is much more constraining: this translates to a 1 σ error of about 0.02 for σ_8 , which is noticeably better than the corresponding value of ~ 0.2 from the CMB ellipse alone.

We now extend Figure 2 to connect, through τ , two a priori independent parameters, $f_{\rm esc}$ and A, shown in Figure 3. The purpose of this plot is to probe the potential of

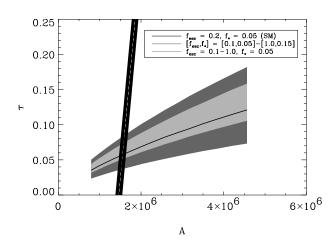


FIG. 2.—Magnified version of Fig. 1; the additional light nested band represents the uncertainty in the value of $f_{\rm esc}$ alone.

cosmology and the astrophysics of reionization to constrain each other, given a reionization model. The ellipse here, as in Figure 1, reveals the inherent degeneracy between τ -related quantities and A through the long narrow ellipse. We now overplot the DSF permitted band for $f_{\rm esc}$ (0.1–0.2); clearly, even this approximate range in $f_{\rm esc}$ considerably narrows the allowed range in A. We note again that our choice of the DSF range for $f_{\rm esc}$ was motivated by the reasons outlined earlier, and that other ranges for $f_{\rm esc}$ are possible; the main point demonstrated by Figure 3 is the power of using any such band of independently known astrophysics to constrain a cosmological parameter. Note also that A would have to be known to great accuracy to place any limits on $f_{\rm esc}$ that are stronger than the DSF band.

So far, we have been using the Fisher matrix formalism for specific pairs of parameters, while fixing the values of the other parameters in the SM. The more general and proper way to do this is to construct a 6×6 matrix for the parameter set $(A, \Omega_b, h, n, f_{esc}, f_*)$, which yields τ . However, the analysis described in § 3 implies that only any five of these six parameters will be independent, since the CMB data will determine the cosmological parameters and τ . Indeed, the 6×6 matrix, when constructed, proves to be singular. We

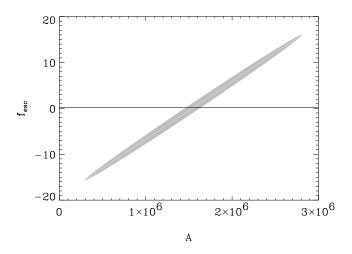


FIG. 3.—Constraint from current CMB data in the $f_{\rm esc}$ -A plane, as extended from Fig. 2; the horizontal band shows the permitted range of 0.1–0.2 for $f_{\rm esc}$ from DSF.

briefly note here some informative aspects of performing singular value decomposition (SVD; Press et al. 1992) of $F_{6\times 6}$, so that $F = UWV^T$, where W is a diagonal 6×6 matrix containing the singular values w. An element that has an anomalously low value (close to zero) in W implies that the corresponding column in V is a linear combination of parameters that will not be well constrained.

Table 1 shows the matrix V with the corresponding column weights w resulting from this decomposition; also shown are the parameters associated with each row in V, where A is expressed as σ_8^2 . We see that the sixth weight is very close to zero, so that the sixth column of V contains combinations of (P_{cosmo}, P_{astro}) that are poorly constrained by this analysis. This column has terms corresponding to essentially only P_{astro} , the dominant contribution coming from f_{esc} . This implies that f_{esc} will not be well determined from the CMB (via τ), given the reionization model considered here. The first five columns of V also convey what combinations of these six parameters will be constrained; we note that f_{esc} has very small contributions in these, i.e., to the information that can be extracted from the CMB. In comparison, f_* can be better determined from the CMB, as seen from columns 1-5, particularly the fifth, where the dominant term is from f_* . This insensitivity of the CMB data to f_{esc} can be traced back to the stellar reionization model we adopted here; variations in f_* affect τ more significantly than do those in f_{esc} (see Figs. 12 and 15 of HL97). The covariance matrix for F can be found by $\mathscr{C} \equiv F^{-1} = VW^{-1}U^T$. Because the ratio of the minimum to the maximum value of W, $\sim 3 \times 10^{-20}$, is very small compared to machine precision, we follow the usual technique of adjusting the anomalously low singular value in W, here w_6 , to zero (Press et al. 1992); despite this, the SVD inversion of F still produces an inaccurate covariance matrix, i.e., $\mathscr{C} \cdot F \neq I.$

We now proceed to work with the independent 5×5 subportions of the full 6×6 matrix, which translates to $P_{\rm cosmo}$ and any one of $P_{\rm astro}$. These 5 \times 5 matrices are inverted, and the 2×2 submatrix of interest is projected into the two-parameter plane as the appropriate error ellipse, which displays the confidence region after marginalizing over the other parameters. The results of this general Fisher matrix analysis are presented below for the idealized specifications of current data and for those expected from *Planck* (\S 3). Only the temperature anisotropies from the CMB are used for Figures 4-11; the polarization information expected from *Planck* is included for Figures 12-13.

Weight:

w

18110.877

9251.715

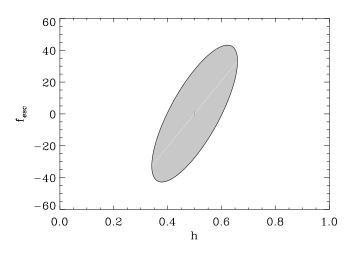


FIG. 4.—Constraints from the CMB in the f_{esc} -h plane; larger ellipse represents current data, and smaller nested ellipse (line) is from Planck.

These plots are intended to be examples of the constraints in various $P_{astro} - P_{cosmo}$ subspaces.

Figure 4 shows the case of f_{esc} versus h; the larger ellipse corresponds to current CMB data, and the nested one (appearing as a tiny line) is from *Planck*. For all subsequent cases, we show these ellipses separately; the astrophysical range for f_{esc} is omitted from this plot for visual clarity. Figure 5 shows the results expected from *Planck* alone for $f_{\rm esc}$ versus h, with the light-shaded horizontal band representing the full range of $f_{\rm esc}$ (0.1–1.0), and the dark band representing the DSF values for $f_{\rm esc}$ (0.1–0.2). The case of $f_{\rm esc}$ versus Ω_b is shown in Figures 6 and 7, for current CMB data and Planck, respectively, with overplotted bands the same as in Figure 5.

Figures 8, 9, 10, and 11 display the respective cases of f_* versus σ_8^2 (where $\sigma_8^2 \propto A$) and f_* versus *n*. For these four plots, the horizontal dark band represents the maximum astrophysical range of 0.01–0.15 for f_* ; values below this range are unlikely to be sufficient for reionization, and values above this range must invoke IMFs other than that of present-day galaxies in order to not violate metal production or background light constraints.

We note here some generic features of Figures 5-11. In all cases, the inclusion of known constraints on the astrophysical parameters strengthens the CMB's limits on cosmological parameters, even for the data expected from *Planck.* This is particularly the case with f_* , due to the

6.366E-16

V and Diagonal Elements of W from $F = UWV^T$ Column Row 1 2 3 4 5 6 -0.39220.1470 -0.51160.7498 -0.02770.000 σ_8^2 -0.0320-0.5024-0.8592-0.00280.0916 8.42E - 16 $\Omega_b \dots$ 0.5012 -0.3673-0.7611-0.1856-0.01113.613E-15 h 0.5840 0.3242 -0.3857 -0.6342-0.05451.599E-14 n 0.0098 -0.00390.0111 0.0041 -0.25390.9671 f_{esc} 0.0373 -0.01480.0420 0.0155 -0.9652-0.2544 f_*

TABLE 1

NOTE.—Results of the singular value decomposition of $F_{6\times 6} = UWV^T$; shown are V, weights w for each column in V, and parameters associated with each row in V.

330.074

12.455

0.0191

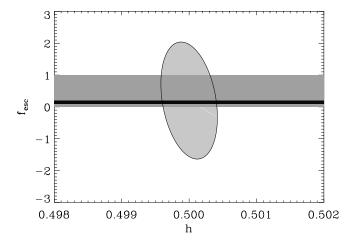


FIG. 5.—Constraint from *Planck* in the f_{esc} -*h* plane; light shaded band represents the entire allowed astrophysical range of 0.1–1.0 for f_{esc} , and the dark shaded band represents the permitted values of 0.1–0.2 for f_{esc} from DSF.

greater sensitivity of τ to f_* relative to f_{esc} . Thus, the 1 σ error for f_* from the CMB is significantly smaller than that for f_{esc} for all the cases shown here, making independent limits on the former a more powerful complementary con-

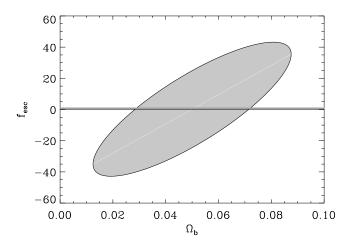


FIG. 6.—Constraint from current CMB data in the $f_{\rm esc}$ - Ω_b plane; shaded bands are the same as in Fig. 5.

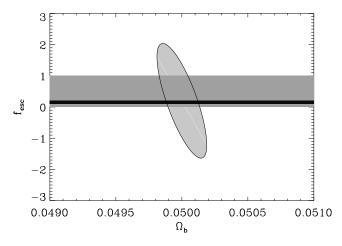


FIG. 7.—Same as Fig. 6, but for data from *Planck*

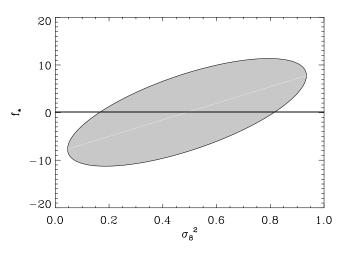


FIG. 8.—Constraint from current CMB data in the $f_* \sigma_8^2$ plane, where $\sigma_8^2 \propto A$; shaded band represents the permitted astrophysical range of 0.01–0.15 for f_* .

straint for cosmological parameters extracted from the CMB. As some illustrative examples involving *Planck* data, the *entire* astrophysical permitted band for f_* reduces the 1 σ error for σ_8 from about 0.02 to less than 0.01 (Fig. 9),

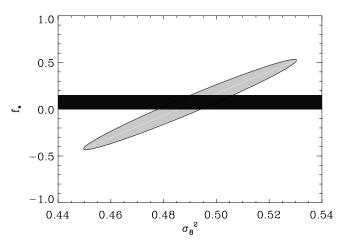


FIG. 9.—Same as Fig. 8, but for data from Planck

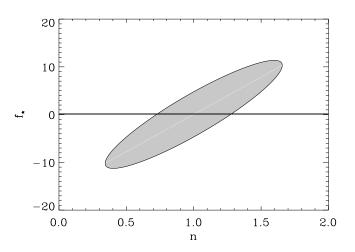


FIG. 10.—Constraint from current CMB data in the f_* -n plane; shaded band is the same as in Fig. 8.

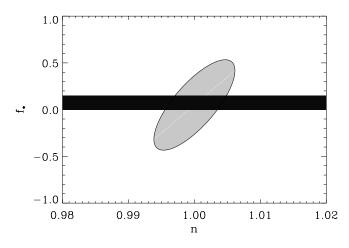


FIG. 11.—Same as Fig. 10, but for data from Planck

and for *n*, from 0.006 to ~0.004. The power to increase such constraints will only become better as f_* (or f_{esc}) become better constrained themselves, but it may not matter much for most cosmological parameters in the post-*Planck* era (since they will already be determined with great precision), with the exception of A or σ_8 . For this case, the method here may prove to be a valuable cross-check.

Figures 5–11 also reveal that even the most promising cases of cosmological parameter determination from the CMB's temperature information will not help to constrain astrophysical parameters such as f_* or f_{esc} , whose currently known ranges as shown through the horizontal bands in each figure are typically much smaller than what would be deduced from the joint confidence region. This is partly due to the low value of τ itself, ~0.06 in our SM, which hinders its accurate determination from the CMB data.

When polarization is included for the projected data from *Planck*, we see, from the two examples shown in Figures 12 and 13, that f_{esc} can be determined to about the same accuracy as the DSF allowed band, but that the 1 σ error for f_* is significantly smaller than its astrophysical uncertainty. Thus, future CMB data may be able to constrain the astrophysical aspects of reionization. We recall, however, that we have neglected effects from experimental noise or from foregrounds in our analysis, which will enlarge the joint con-

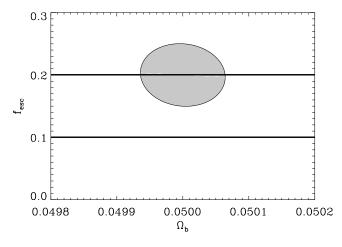


FIG. 12.—Constraint from *Planck* in the $f_{\rm esc}$ - Ω_b plane using temperature and polarization; lines represent the allowed range for $f_{\rm esc}$ from DSF.

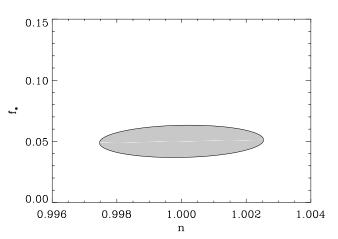


FIG. 13.—Constraint from *Planck* in the f_* -*n* plane using temperature and polarization; the allowed astrophysical range for f_* is the entire y-axis.

fidence regions in all the figures. While this only strengthens the argument for the power of astrophysical limits in constraining cosmology, the converse situation, which appears hopeful from Figures 12–13, is realistically tentative at best. In short, it is possible in principle that the astrophysics of a stellar reionization model can be constrained by limits on cosmological parameters from *Planck*'s temperature and polarization data, although this may prove difficult to achieve. We may simply have to await the view from *SIRTF* and the *NGST* to determine the reionizing activity of the first stars.

5. CONCLUSIONS

We have examined the power of a reionization model, given its many cosmological and astrophysical parameters, to constrain these input quantities when combined with parameter extraction from the CMB. In the case of the well-known degeneracy between τ and A in their effects on the CMB, we have found that this can be alleviated by the complementary information from a reionization model, and that this remains a useful cross-constraint even when allowing for the astrophysical uncertainty in τ .

When we eliminate τ and perform a more general Fisher matrix analysis, we find that the astrophysical details of reionization *can* be useful in further constraining the CMB's limits on cosmological parameters, even in the case of the expected temperature data from *Planck*. We have shown that independent limits on the astrophysical inputs to reionization, despite the current uncertainty in their values, reduce the errors for cosmological parameters by a factor of at least ~2. Given that we have considered the most optimistic parameter yield from CMB experiments (§ 3), the use of known astrophysics can only become more valuable for realistic experimental results. This is of particular value for σ_8 (or A) and n, given their implications for structure formation and for theoretical models of the origin of the seeds of structure in the early universe.

The converse situation—using a projected exquisite determination of a cosmological parameter to constrain astrophysical reionization parameters—does not yield quite as interesting results with temperature data from current experiments or from *Planck*, even though we made the most optimistic assumptions; the 1 σ errors for f_{esc} or f_* are larger than what are already known to be reasonable. When the projected polarization data from *Planck* is included, we

found that f_* in particular can be constrained to far greater accuracy than its current astrophysical uncertainty; in practice, however, this may prove difficult to achieve, given the effects of foregrounds and instrumental noise, which we have neglected here.

In summary, the astrophysical details of reionization can strengthen the limits on the cosmology of our universe, beyond even the projected parameter yield from future CMB data, and there is more potential to a measurement of τ than the determination of a single number out of a large parameter space describing adiabatic CDM models. These broad conclusions are naturally subject to the assumptions made in this analysis. The sizes of joint confidence regions derived from the CMB data for any two-parameter subspace is determined by the full covariance matrix, whose elements' values are dependent on the dimension of the chosen parameter space and the selected parameters. The inclusion of more parameters has the generic result of increasing the sizes of the error ellipses; therefore, the primary results of this paper can only be strengthened when parameter spaces larger than that analyzed here are considered.

In the SCDM cosmology assumed here, the values of τ in our standard model were relatively low (~ 0.06). In an open universe, or one dominated by a cosmological-constant

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contribution, we expect larger average values of τ for a fixed reionization model, since structures freeze out earlier, resulting in a longer line of sight to the last scattering surface at the reionization epoch. Increased τ 's can also result from higher values of f_* or f_{esc} , or from a lower value of M_C (§ 2), which would allow the first stars to form earlier and more ubiquitously. Since higher τ 's will have a better chance of being accurately determined from the CMB, it would be interesting to analyze the constraints in this paper, from both the reionization scenario and the CMB, for a more general parameter space; we examine this in a forthcoming work.

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